

## Determining the coefficient of static friction using the inclined plane

### Objects of the experiment

- Determining the coefficient of static friction  $\mu$  from the equilibrium between the force along the plane and the static friction force on an inclined plane

### Principles

A body on an inclined plane with the weight  $G$  is subject to a force along the plane (parallel to the plane) of

$$F_1 = G \cdot \sin \alpha \quad (I)$$

and to a force normal (perpendicular) to the plane of

$$F_2 = G \cdot \cos \alpha \quad (II)$$

This dependency on the angle of inclination  $\alpha$  can be used to determine quantitatively the coefficient of friction  $\mu$  of the body. The angle of inclination of the plane is increased by moving the support until the body just begins to slide, i.e. the force  $F_1$  along the plane and the static friction force  $F$  are in equilibrium. In this experiment the tangent of the angle of inclination is determined from the height  $h = 5$  cm of the support and its distance  $s$  from the pivot of the inclined plane are measured.

$$\tan \alpha = \frac{h}{s} \quad (III)$$

The static friction force is generally taken to be proportional to the force  $F_2$  along the plane:

$$F = \mu \cdot F_2 \quad (IV)$$

From the equilibrium of forces  $F_1 = F$  we can deduce:

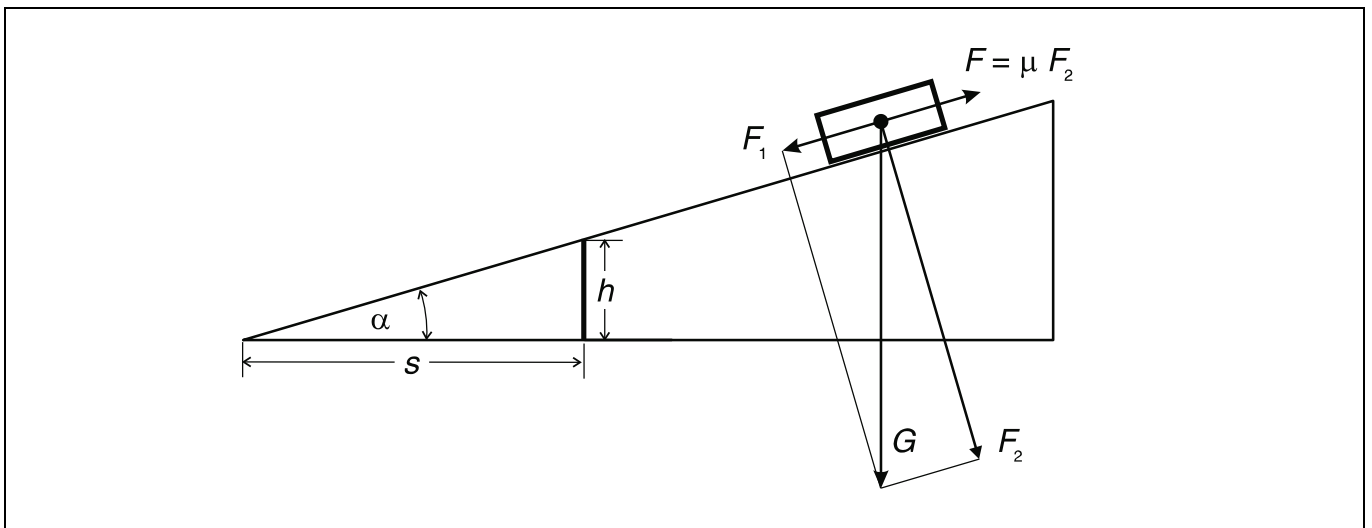
$$F_1 = \mu \cdot F_2 \quad (V)$$

$\mu$ : coefficient of friction

and thus from (I), (II) and (III)

$$\mu = \frac{h}{s} \quad (VI).$$

Fig. 1 Equilibrium between the force  $F_1$  along the plane and the static friction force  $F$  on an inclined plane.



**Apparatus**

1 Inclined plane with trolley and screw model . . . . .	341 21
1 Pair of wooden blocks for friction experiments . . . . .	342 10

**Setup and carrying out the experiment**

- Set up the inclined plane and move the support (a) to the farthest possible point from the pivot.
- Place block 1 (6 cm thick) on the inclined plane with the plastic-coated side down and slowly move the support inward until the block starts to slide.
- Measure the distance between the pivot and the support using the tape measure and calculate the coefficient of static friction using equation (VI).
- Place block 1 on the plane with the wooden side down and repeat the experiment.
- Place block 2 (3 cm thick) on the inclined plane with the plastic-coated side down and repeat the experiment.
- Turn the wooden surface with the area  $A = 12 \times 6 \text{ cm}^2$  down and repeat the experiment.
- Turn the wooden surface with the area  $A = 12 \times 3 \text{ cm}^2$  down and repeat the experiment.

**Measuring example and evaluation**

Block	Material	$\frac{A}{\text{cm}^2}$	$\frac{s}{\text{cm}}$	$\mu$
1	Plastic	$12 \times 6$	10.5	0.48
1	Wood	$12 \times 6$	21.9	0.23
2	Plastic	$12 \times 6$	9.5	0.53
2	Wood	$12 \times 6$	20.7	0.24
2	Wood	$12 \times 3$	21.1	0.24

**Results**

The coefficient of static friction depends on the material of the contact surface, but not on its surface area.

Fig. 2 Experiment setup for determining the coefficient of friction on an inclined plane

